

Degree Based Topological Indices of Vitamins

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Abstract— This article is mainly focused on calculating degree based topological indices of some vitamins by edge partition of graphs vitamin K and vitamin E by using First Zagreb index, Second Zagreb index, Harmonic index, Atom Bond Connectivity (ABC) index, Sum connectivity index, Sigma index and Albertson index.

Index Terms: Topological indices, Vitamin K, Vitamin E, Harmonic index, Atom Bond Connectivity index.

I. INTRODUCTION

Organic compounds like vitamins are very essential for human body to function well, a small quantity of vitamins are essential for body functioning[1]. Vitamin K is a fat soluble vitam in it is very useful for many body functions such as blood coagulation, bone mineralization and insulin sensitization. It is also found in some foods and is also available as a dietary supplement [2].

Vitamin K plays a very important role in proper functioning of liver and prevents excessive bleeding and helps in clotting of blood. It is also important for healthy bones. Vitamin K gets stored in the liver, so that one can need not eat it every day like other vitamins [3][4].

Vitamin E is a fat soluble, it exists in several foods like vegetable oil, cereals, meat, poultry, eggs and fruits. This vitamin helps in proper functioning of majority of organs. It also acts as an antioxidants [5][6]. Rich vitamin E foods are canola oil, olive oil, margarine, almonds and peanuts. Vitamin E is also available from meat, dairy, green leafy vegetables.

Topological index is a molecular descriptor it can be used to predict a particular value of a graph. from this index one can analyze mathematical values and further investigate some physicochemical properties of a molecule [7].

Consider a simple connected graph G with vertices V is denoted as a set $v_1, v_2, v_3, \dots, v_n$ and edges E denoted as a set $e_1, e_2, e_3, \dots, e_n$ the degree of the vertex d_u is the number of neighbor vertices of G .

II. LITERATURE REVIEW

A. First and second zagreb index:

The First Zagreb index $M_1(G)$ and second Zagreb index $M_2(G)$, are the first degree based topological indices invented by Gutman and Trinajsti in 1972 and these indices are defined as[8].

$$M_1(G) = \sum_{u,v \in E(G)} (d_u + d_v)$$

$$M_2(G) = \sum_{u,v \in E(G)} (d_u * d_v)$$

B. Atom Bond Connectivity index:

One of the familear connectivity index is the Atom Bond connectivity (ABC) it was introduced by Estrada et.al [9] and is defined as

$$ABC(G) = \sum_{u,v \in E(G)} \sqrt{\frac{d_u + d_v - 2}{d_u d_v}}$$

C. Harmonic index:

In 1980's Siemion Fajtlowicz introduced a new topological indicator and named as Harmonic index and is defined as the weights $\frac{2}{d_u + d_v}$ of all edges u, v of G , where d_u denotes the degree of a vertex u in G [10].

$$H(G) = \sum_{u,v \in E(G)} \frac{2}{d_u + d_v}$$

D. Sum connectivity index:

The sum connectivity index was introduced by Nenad Trinajstic and Bo Zhou. It is defined as[11]

$$SCI(G) = \sum_{u,v \in E(G)} \frac{1}{\sqrt{d_u + d_v}}$$

E. Sigma index:

Amer et. Al introduced the Sigma index in 1900 which is defined as [12]

$$\sigma(G) = \sum_{u,v \in E(G)} (d_u - d_v)^2$$

F. Albertson index:

In 1997, the Albertson index of connected graph G , introduced by Albertson, is defined as,[13]

$$Alb(G) = \sum_{u,v \in E(G)} |d_u - d_v|$$

III. MAIN RESULTS

A. Topological indices of vitamin K (C₃₁H₄₀O₂):

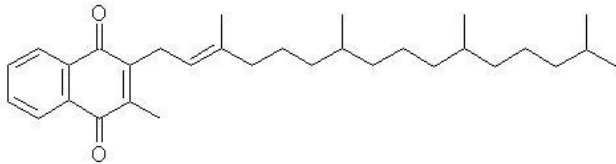


Fig. 1. Chemical structure of vitamin K (C₃₁H₄₀O₂)

From fig 1, the chemical structure of vitamin K $e_{i,j}$ denotes the edges connecting the vertices d_i and d_j . Two dimensional structure containing edges of the type

$$e(2,2) = 10, e(3,3) = 6, e(2,3) = 10 \text{ and } e(1,3) = 8$$

Theorem 1: Prove the first and second Zagreb index of vitamin K (C₃₁H₄₀O₂) are $M_1(G) = 158$ and $M_2(G) = 178$

Proof: $M_1(G) = \sum_{u,v \in E(G)} (d_u + d_v)$
 $= e(2,2). (2 + 2) + e(3,3). (3 + 3) + e(2,3). (2 + 3) + e(1,3). (1 + 3)$
 $= 10(4) + 6(6) + 10(5) + 8(4)$
 $= 158$

$$M_2(G) = \sum_{u,v \in E(G)} (d_u * d_v)$$

$$= e(2,2). (2*2) + e(3,3). (3*3) + e(2,3). (2*3) + e(1,3). (1*3)$$

 $= 10(4) + 6(9) + 10(6) + 8(3)$
 $= 178$

Theorem 2: The Atom bond connectivity index of vitamin K (C₃₁H₄₀O₂) is 25.5731

Proof: $ABC(G) = \sum_{u,v \in E(G)} \sqrt{\frac{d_u + d_v - 2}{d_u d_v}}$
 $= e(2,2) \cdot \sqrt{\frac{2+2-2}{2*2}} + e(3,3) \cdot \sqrt{\frac{3+3-2}{3*3}} + e(2,3) \cdot \sqrt{\frac{2+3-2}{2*3}}$
 $+ e(1,3) \cdot \sqrt{\frac{1+3-2}{1*3}}$
 $= 25.5731$

Theorem 3: The Harmonic index of vitamin K (C₃₁H₄₀O₂) is 15

Proof: $H(G) = \sum_{u,v \in E(G)} \frac{2}{d_u + d_v}$
 $= e(2,2). (\frac{2}{2+2}) + e(3,3). (\frac{2}{3+3}) + e(2,3). (\frac{2}{2+3}) + e(1,3). (\frac{2}{1+3})$
 $= 15$

Theorem 4: The Sum connectivity index of vitamin K (C₃₁H₄₀O₂) is 16.4721

Proof: $SCI(G) = \sum_{u,v \in E(G)} \frac{1}{\sqrt{d_u + d_v}}$
 $= e(2,2). (\frac{1}{\sqrt{2+2}}) + e(3,3). (\frac{1}{\sqrt{3+3}}) + e(2,3). (\frac{1}{\sqrt{2+3}}) + e(1,3). (\frac{1}{\sqrt{1+3}})$
 $= 16.4721$

Theorem 5: The sigma index of vitamin K (C₃₁H₄₀O₂) is 282

Proof: $\sigma(G) = \sum_{u,v \in E(G)} (d_u - d_v)^2$
 $= e(2,2). (2 - 2)^2 + e(3,3). (3 - 3)^2 + e(2,3). (2 -$

$$3)^2 + e(1,3). (1 - 3)^2$$

 $= 282$

Theorem 6: The Albertson index of vitamin K (C₃₁H₄₀O₂) is 66

Proof: $Alb(G) = \sum_{u,v \in E(G)} |d_u - d_v|$
 $= e(2,2). |2 - 2| + e(3,3). |3 - 3| + e(2,3). |2 - 3| + e(1,3). |1 - 3|$
 $= 66$

B. Results of vitamin E

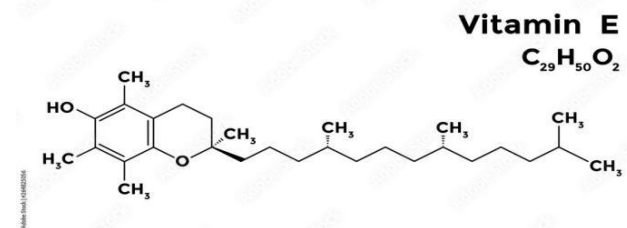


Fig. 2. Chemical structure of vitamin E

From the above structure of vitamin E let $e_{i,j}$ denotes the edges connecting the vertices d_i and d_j . Two dimensional structure containing edges of the type

$$e(2,2) = 7, e(3,3) = 6, e(2,3) = 2, e(1,3) = 8, e(2,4) = 3 \text{ and } e(1,4) = 1$$

Theorem 1: The first and second Zagreb index of vitamin E (C₂₉H₅₀O₂) are $M_1(G) = 129$

and $M_2(G) = 146$

Proof: $M_1(G) = \sum_{u,v \in E(G)} (d_u + d_v)$
 $= e(2,2). (2 + 2) + e(3,3). (3 + 3) + e(2,3). (2 + 3) + e(1,3). (1 + 3) + e(1,4). (1 + 4) + e(2,4). (2 + 4)$
 $= 7(4) + 6(6) + 2(5) + 8(4) + 1(5) + (6)$
 $= 129$

$$M_2(G) = \sum_{u,v \in E(G)} (d_u * d_v)$$

$$= e(2,2). (2*2) + e(3,3). (3*3) + e(2,3). (2*3) + e(1,3). (1*3) + e(1,4). (1*4) + e(2,4). (2*4)$$

 $= 7(4) + 6(9) + 2(6) + 8(3) + 1(4) + 3(8)$
 $= 146$

Theorem 2: The Atom bond connectivity index of vitamin E (C₂₉H₅₀O₂) is 19.8832

Proof: $ABC(G) = \sum_{u,v \in E(G)} \sqrt{\frac{d_u + d_v - 2}{d_u d_v}}$
 $= e(2,2). \sqrt{\frac{2+2-2}{2*2}} + e(3,3). \sqrt{\frac{3+3-2}{3*3}} + e(2,3). \sqrt{\frac{2+3-2}{2*3}}$
 $+ e(1,3). \sqrt{\frac{1+3-2}{1*3}} + e(1,4). \sqrt{\frac{1+4-2}{1*4}} + e(2,4). \sqrt{\frac{2+4-2}{2*4}}$
 $= 19.8832$

Theorem 3: The Harmonic index of vitamin E (C₂₉H₅₀O₂) is 12.9

Proof: $H(G) = \sum_{u,v \in E(G)} \frac{2}{d_u + d_v}$
 $= e(2,2). (\frac{2}{2+2}) + e(3,3). (\frac{2}{3+3}) + e(2,3). (\frac{2}{2+3}) + e(1,3). (\frac{2}{1+3})$

$$+e(1, 4) \cdot \left(\frac{2}{1+4}\right) + e(2, 4) \cdot \left(\frac{2}{2+4}\right) = 12.9$$

Theorem 4: The Sum connectivity index of vitamin E ($C_{29}H_{50}O_2$) is 11.2676

Proof: $SCI(G) = \sum_{u,v \in E(G)} \frac{1}{\sqrt{d_u + d_v}}$

$$[1]. = e(2, 2) \cdot \left(\frac{1}{\sqrt{2+2}}\right) + e(3, 3) \cdot \left(\frac{1}{\sqrt{3+3}}\right) + e(2, 3) \cdot \left(\frac{1}{\sqrt{2+3}}\right) + e(1, 3) \cdot \left(\frac{1}{\sqrt{1+3}}\right) + e(1, 4) \cdot \left(\frac{1}{\sqrt{1+4}}\right) + e(2, 4) \cdot \left(\frac{1}{\sqrt{2+4}}\right) = 11.2676$$

Theorem 5: The sigma index of vitamin E ($C_{29}H_{50}O_2$) is 55

Proof: $\sigma(G) = \sum_{u,v \in E(G)} (d_u - d_v)^2$

$$= e(2, 2) \cdot (2 - 2)^2 + e(3, 3) \cdot (3 - 3)^2 + e(2, 3) \cdot (2 - 3)^2 + e(1, 3) \cdot (1 - 3)^2 + e(1, 4) \cdot (1 - 4)^2 + e(2, 4) \cdot (2 - 4)^2 = 55$$

Theorem 6: The Albertson index of vitamin E ($C_{29}H_{50}O_2$) is 27

Proof: $Alb(G) = \sum_{u,v \in E(G)} |d_u - d_v|$

$$= e(2, 2) \cdot |2 - 2| + e(3, 3) \cdot |3 - 3| + e(2, 3) \cdot |2 - 3| + e(1, 3) \cdot |1 - 3| + e(1, 4) \cdot |1 - 4| + e(2, 4) \cdot |2 - 4| = 27$$

IV. CONCLUSION

In this article we computed degree based topological indices of vitamins. These indices serve as a valuable tool for calculating physicochemical traits of drugs. These findings contribute significantly to our understanding of the mathematical aspects.

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